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Special Colloquium
of
Fundamental Research Department

27 June 2022

Future prospects to shed
light on cosmic mysteries

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Measuring the viscosity of dark matter with strongly lensed gravitational waves

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Hubble diagram at higher redshifts: model independent calibration of quasars

Xiaolei Li,^{1*} Ryan E. Keeley,^{2*} Arman Shafieloo^{2,3*}, Xiaogang Zheng,⁴ Shuo Cao,⁵ Marek Biesiada^{5,6} and Zong-Hong Zhu⁵

Measurements of the Hubble constant and cosmic curvature with quasars: ultracompact radio structure and strong gravitational lensing

Jing-Zhao Qi,¹ Jia-Wei Zhao,¹ Shuo Cao,^{2*} Marek Biesiada³ and Yuting Liu²

Dark matter (satellite) halo mass deficit?

1. **Dark matter cores** of kpc size are preferred by observed circular velocities in dwarf/low-surface-brightness (LSB) galaxies, while simulations suggest cusps [Moore 1994; Burkert 1995, ...].

(core/cusp problem)

2. **Non-observation of very massive satellite halos** predicted by simulations in our Milky Way [M.Boylan-Kolchin et al. 2011, 2012] and others [Ferrero et al. 2011].

(too-big-to-fail problem)

3. Given the long lifetime of dwarfs, some globular/star clusters are expected to be destroyed, or sink to the center **if their host halos are cuspy** [J. Binney & S.Tremaine 2008, F. Contenta et al. 2017, P. Boldrini et al. 2018, ...].

(GC timing problem)

Self-interacting dark matter (SIDM)?

- Stronger self-scattering needed for (dwarf-sized) halos

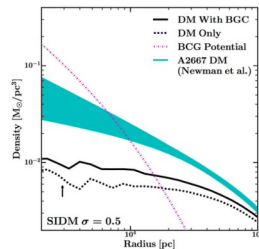
[O. D. Elbert et al. 2016, K. Bondarenko 2016, ...]

😊 $\frac{\sigma_{SI}}{m_{DM}} \sim 0.5 - 10 \text{ cm}^2/\text{g}$ at dwarf scales of DM velocity $\sim 10 \text{ km/s}$

- Weaker self-scattering favored by cluster merging/halo profiles etc.

[O. D. Elbert et al. 2016, K. Bondarenko 2016, ...]

😓 $\frac{\sigma_{SI}}{m_{DM}} \leq 0.2 - 1 \text{ cm}^2/\text{g}$ at cluster scales of DM velocity $\sim 1000 \text{ km/s}$



More heat/entropy needed in halo centre (if confirmed)

Heat needed to make a kpc dark core: $10^{53} - 10^{55} \text{ erg}$

- Baryonic effects?** heated by supernova / in-falling clumps.

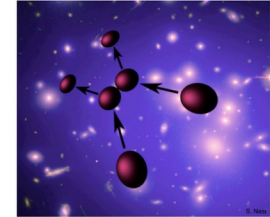
Each supernova deposits $\sim 10^{51} \text{ erg}$ in interstellar medium [e.g. Madau, Shen, Governato 2014, ...]

- Self-interacting dark matter?** (also decaying / fuzzy dark matter, ...)

Observational evidence for self-interacting cold dark matter

D.N. Spergel and P.J. Steinhardt [astro-ph/9909386]

Infalling dark matter is scattered before reaching the center of the galaxy so that the orbit distribution is isotropic rather than radial. **These collisions increase the entropy of the dark matter phase space distribution and lead to a dark matter halo profile with a shallower density profile.**



O(1) scattering per (central) particle $\longrightarrow \frac{\sigma_{SI}}{m_{DM}} \sim 0.5 - 10 \text{ cm}^2/\text{g}$

Plane GW Traveling Through Homogeneous Matter

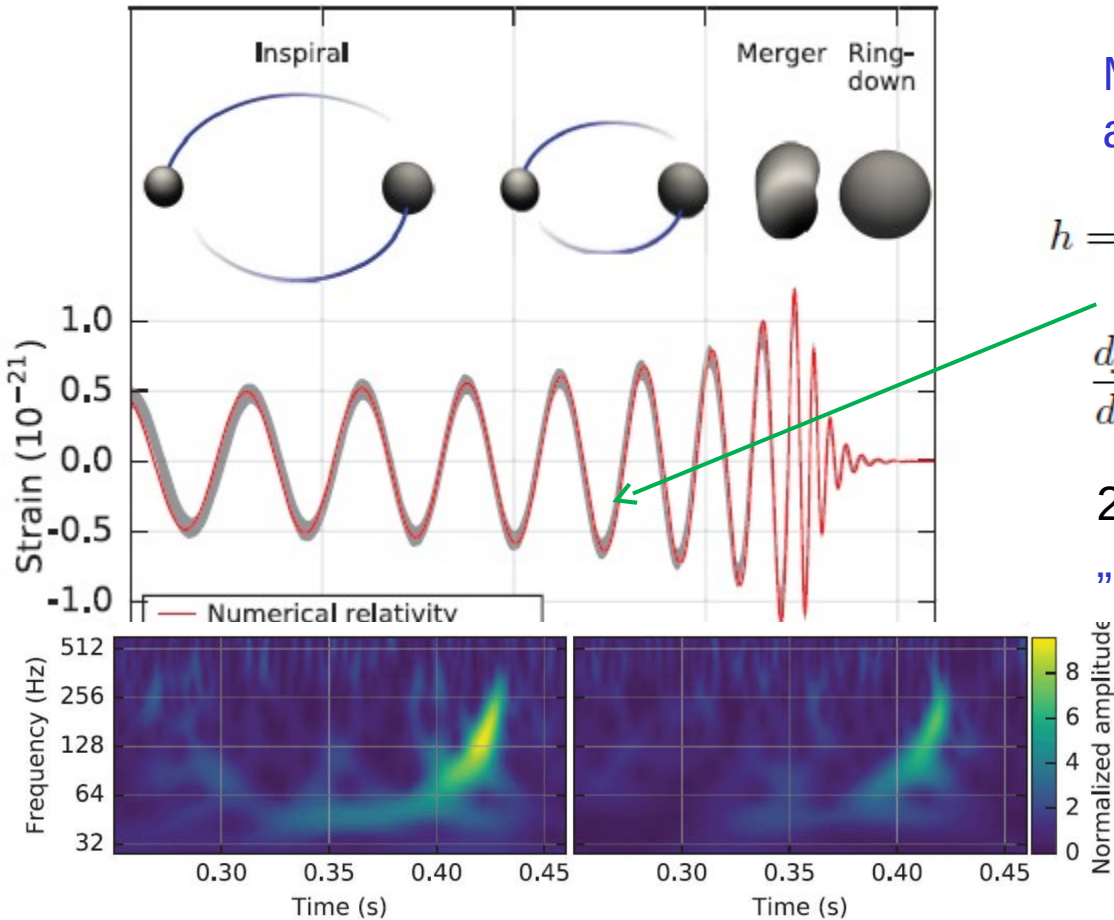
- Fluid:**

- GW shears the fluid, (rate of shear) = $\sigma_{jk} = \frac{1}{2} \dot{h}_{jk}^{GW}$
- no resistance to shear, so no action back on wave
- Viscosity $\eta \sim \rho v s = (\text{density})(\text{mean speed of particles})(\text{mean free path})$ produces stress $T_{jk} = -2\eta\sigma_{jk} = -\eta \dot{h}_{jk}^{GW}$ **NOTE:** s must be $< \lambda$
- Linearized Einstein field equation: $\square h_{jk}^{GW} = -16\pi(T_{jk})^{TT} = 16\pi\eta \dot{h}_{jk}^{GW}$
- Wave attenuates: $h_{jk}^{GW} \sim \exp(-z/\ell_{att})$ where $\ell_{att} = \frac{1}{8\pi\eta} = \frac{1}{8\pi\rho v s}$

The idea of „standard sirens”

B. Schutz 1986

B.Schutz, A. Królak 1987



Measure the strain $h(t)$
and frequency drift df/dt

$$h = \frac{4\pi^{2/3}(GM)^{5/3}}{c^4 D} f(t)^{2/3} \cos \left[\int_0^t f(t') dt' \right]$$

$$\frac{df}{dt} = \frac{96\pi^{8/3}}{5} \left(\frac{GM}{c^3} \right)^{5/3} f^{11/3}$$

2 equations for 2 unknowns:
„chirp mass” M & distance D

$$\mathcal{M} = \frac{c^3}{G} \left(\frac{5}{96\pi^{8/3}} \frac{df}{dt} \right)^{3/5} f^{-11/5}$$

$$D = \frac{4c}{\pi^2 h} \frac{df(t)}{dt} f^{-3} \cos \left(\int_0^t f(t') dt' \right)$$

for cosmological sources

$$M_c \rightarrow (1+z) M_c$$

$$t \rightarrow (1+z)t$$

$$f \rightarrow \frac{1}{1+z} f$$

$$\frac{df}{dt} \rightarrow \frac{1}{(1+z)^2} \frac{df}{dt}$$

The distance inferred is the **luminosity distance**

$$D_L = (1+z) D \quad 5$$

Measuring the viscosity of dark matter with strongly lensed gravitational waves

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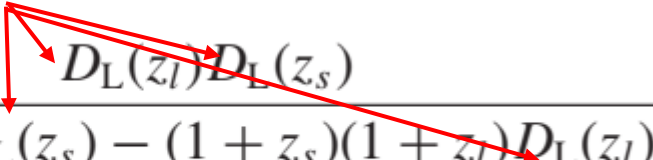
⁴Department of physics, Chongqing University, 400044 Chongqing, China

$$h_{\alpha, \text{visc}} = h_{\alpha} e^{-\beta D/2} \quad \text{attenuated wave leads to biased luminosity distance} \quad D_{L, \text{eff}}(z, \beta) = D_L(z) e^{\beta D(z)/2}$$

lensed transients (GW, SNIa) signal leads to very precise determination of „time delay distance”

$$\Delta t_{i,j} = \frac{D_{\Delta t}(1+z_l)}{c} \Delta \phi_{i,j} \quad D_{\Delta t}(z_l, z_s) \equiv \frac{D_A(z_l)D_A(z_s)}{D_A(z_l, z_s)}$$

To be determined by unlensed standard sirens

$$D_{\Delta t} = \frac{D_L(z_l)D_L(z_s)}{(1+z_l)^2 D_L(z_s) - (1+z_s)(1+z_l)D_L(z_l)}$$


objective function fitted for beta

$$\chi^2 = \sum_{i=1}^i \frac{(D_{\Delta t,i}^{lens}(z_{l,i}, z_{s,i}) - D_{\Delta t,i}^{unlens}(z_{l,i}, z_{s,i}; \beta))^2}{\sigma_{i,lens}^2 + \sigma_{i,unlens}^2}$$

relation with DM physical parameters

$$\frac{\langle \sigma_\chi \rangle}{m_\chi} = \frac{6.3\pi G \langle v \rangle}{c^3 \beta}$$

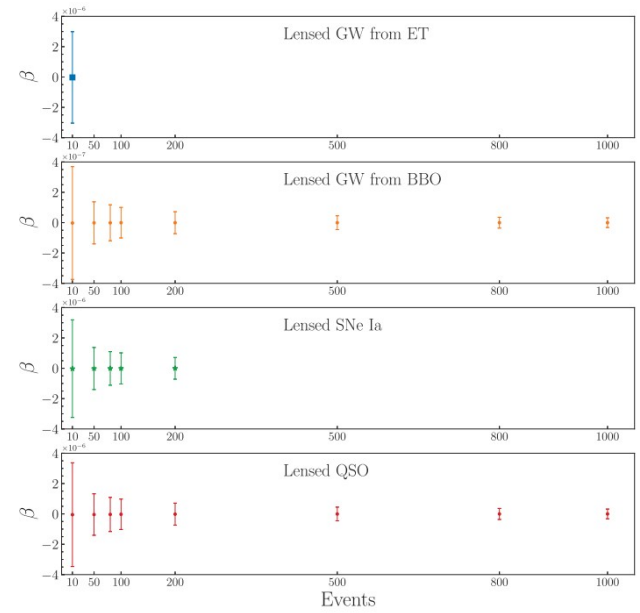


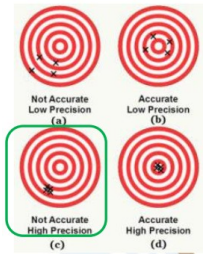
Table 1. Summary of the constraints obtained from different observations. Type I and II, respectively, correspond to the two cases of self-interacting DM in galaxies and galaxy clusters.

Data	$\Delta\beta$	$\Delta(\sigma_\chi/m_\chi)(I)$	$\Delta(\sigma_\chi/m_\chi)(II)$
GW (lensed; ET) + GW (unlensed)	10^{-6} Mpc^{-1}	$10^{-4} \text{ cm}^2 \text{ g}^{-1}$	$10^{-3} \text{ cm}^2 \text{ g}^{-1}$
GW (lensed; BBO) + GW (unlensed)	10^{-8} Mpc^{-1}	$10^{-6} \text{ cm}^2 \text{ g}^{-1}$	$10^{-5} \text{ cm}^2 \text{ g}^{-1}$
QSO (lensed; LSST) + GW (unlensed)	10^{-7} Mpc^{-1}	$10^{-5} \text{ cm}^2 \text{ g}^{-1}$	$10^{-4} \text{ cm}^2 \text{ g}^{-1}$
SNe Ia (lensed; LSST) + GW (unlensed)	10^{-6} Mpc^{-1}	$10^{-4} \text{ cm}^2 \text{ g}^{-1}$	$10^{-3} \text{ cm}^2 \text{ g}^{-1}$

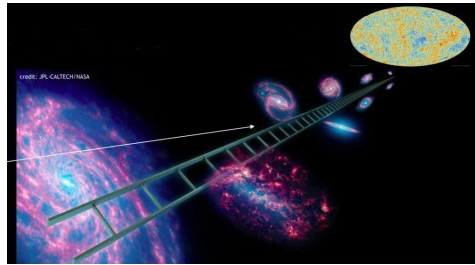
it would be able to DM viscosity and differentiate cluster and small scale scenarios

Measurements of the Hubble constant and cosmic curvature with quasars: ultracompact radio structure and strong gravitational lensing

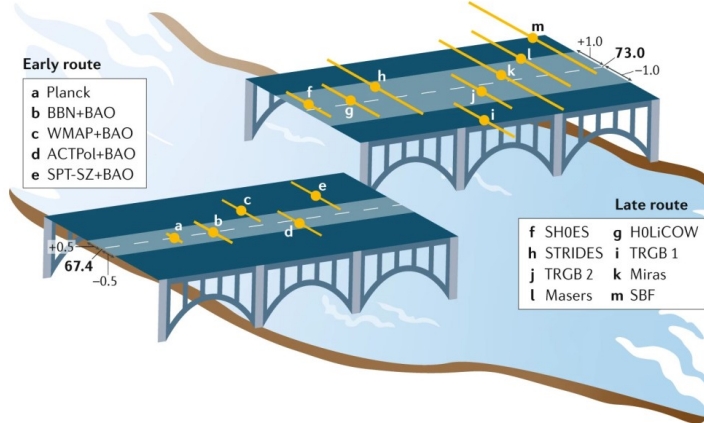
Jing-Zhao Qi,¹ Jia-Wei Zhao,¹ Shuo Cao,²★ Marek Biesiada³ and Yuting Liu²



H_0 tension



Credits: JPL-Caltech/NASA and Dillon Brout



Credits: Riess, Nat. Rev. Phys. 2 (2020) 10

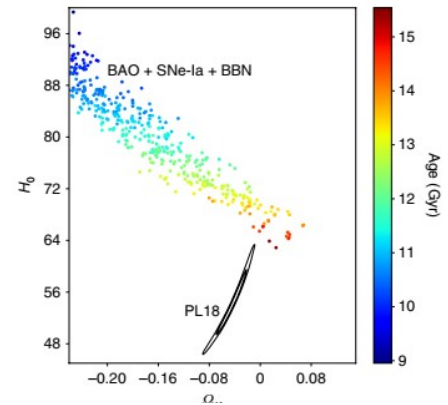
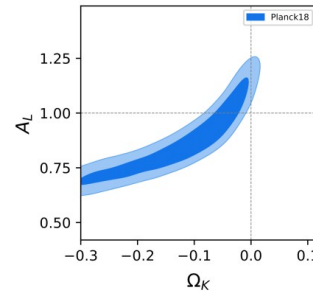
ARTICLES

<https://doi.org/10.1038/s41550-019-0906-9>

nature
astronomy

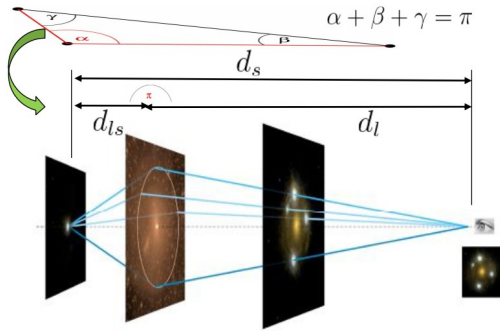
Planck evidence for a closed Universe and a possible crisis for cosmology

Eleonora Di Valentino¹, Alessandro Melchiorri^{2*} and Joseph Silk^{3,4,5}



the preference at 3.4σ for a closed Universe

$$\Omega_K = -0.044^{+0.018}_{-0.015}$$



$$d_{ls} = \sqrt{1 + \Omega_k d_l^2} d_s - \sqrt{1 + \Omega_k d_s^2} d_l$$

One can obtain Ω_k and H_0 if

d_l, d_s, d_{ls} are known

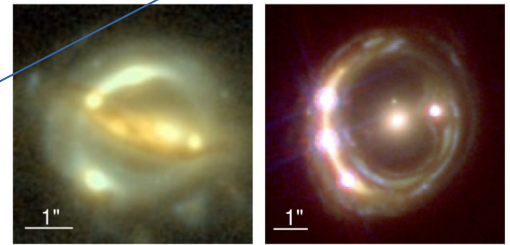
Observations:
 z_l, z_s – known

Time delays -- $> d_l d_s / d_{ls}$

=====
 $d_l d_s$ – standard candle or ruler
matched by redshift

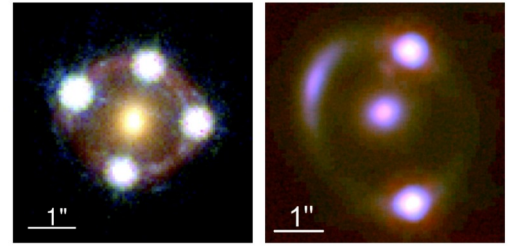
HOLICOW six well studied lenses

$$D_{\Delta t} = \frac{c \Delta t_{i,j}}{\Delta \phi_{i,j}} = \frac{c}{H_0} \frac{d_l d_s}{d_{ls}}$$



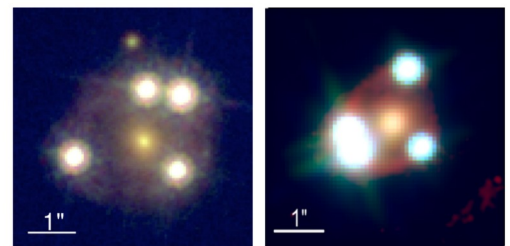
(a) B1608+656

(b) RXJ1131-1231



(c) HE 0435-1223

(d) SDSS 1206+4332



(e) WF12033-4723

(f) PG 1115+080

$$\frac{d_l d_s}{d_{ls}} = \frac{1}{\sqrt{1/d_l^2 + \Omega_k} - \sqrt{1/d_s^2 + \Omega_k}}$$

Instead of simple matching by z
we used $d(z)$ reconstructed from
ILQSO

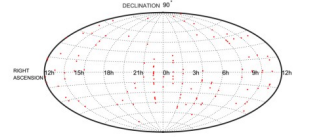
ARA 606, A15 (2017)
DOI: 10.1017/0004-6361/20170551
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Astronomy
Astrophysics

Compact radio sources

Ultra-compact structure in intermediate-luminosity radio quasars:
building a sample of standard cosmological rulers and improving
the dark energy constraints up to $z \sim 3$

Shao Cao¹, Xiangang Zheng^{1,2}, Marek Biesiada^{1,2}, Jinghao Qi¹, Yun Chen², and Zong-Hong Zhu¹

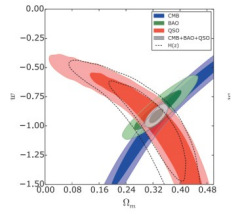


120 compact radio sources (QSOs)
at 2 GHz

- Steps:
1. expansion rate reconstruction from $H(z)$ data (cosmic chronometers)
 2. robust selection of luminosity sample
 3. calibration of standard rulers $l = 11.03 \pm 0.25$ pc

4. $D_A(z)$ reconstruction (GP) from binned ILQSO data or use of calibrated ILQSO for cosmological parameter inference

$$\theta(z) = \frac{l_m}{D_A(z)}$$



$$\chi_{\text{QSO}}^2 = \sum_i \frac{[\theta(z_i; d(z_i)) - \theta_{oi}]^2}{\sigma_i^2}$$

$$\mathcal{L}_{\text{QSO}} \sim \exp(-\chi_{\text{QSO}}^2/2)$$

$$\ln \mathcal{L} = \ln(\mathcal{L}_{\text{QSO}}) + \ln(\mathcal{L}_{\Delta t})$$

$$0.654 < z_s < 2.375.$$

Table 1. Summary of the best-fitting values and the corresponding BIC for the Hubble constant (H_0), cosmic curvature (Ω_K), and the coefficients of third-order polynomial expansion (a_1 , a_2), with strongly lensed and unlensed radio quasars in the framework of distance sum rule.

H_0 (km s ⁻¹ Mpc ⁻¹)	Ω_K	a_1	a_2	BIC
78.3 ± 2.9	0.49 ± 0.24	-0.365 ± 0.037	0.069 ± 0.014	492.2
73.6 ± 1.7	0 (fixed)	-0.404 ± 0.030	0.077 ± 0.013	491.0
74.03 (fixed)	$0.22^{+0.14}_{-0.17}$	-0.412 ± 0.018	0.084 ± 0.010	489.3

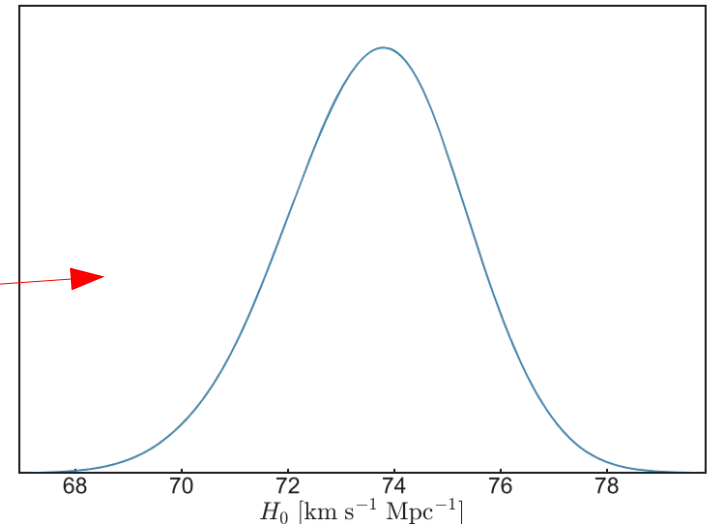
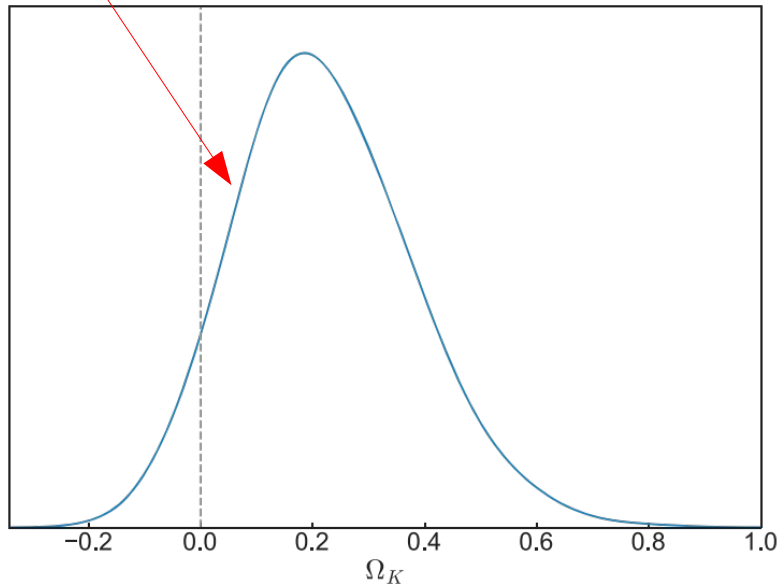
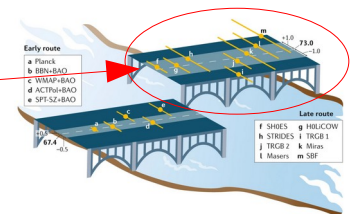


Table 3. Summary of the best-fitting values for the Hubble constant (H_0), matter density parameter (Ω_m) and cosmic curvature (Ω_K), with strongly lensed and unlensed radio quasars in the framework of non-flat Λ CDM and flat Λ CDM model.

	H_0 (km s ⁻¹ Mpc ⁻¹)	Ω_K	Ω_m
Non-flat Λ CDM	72.5 ± 1.6	$-0.09^{+0.13}_{-0.15}$	0.287 ± 0.055
Flat Λ CDM	$73.1^{+1.5}_{-1.3}$	—	$0.254^{+0.027}_{-0.035}$

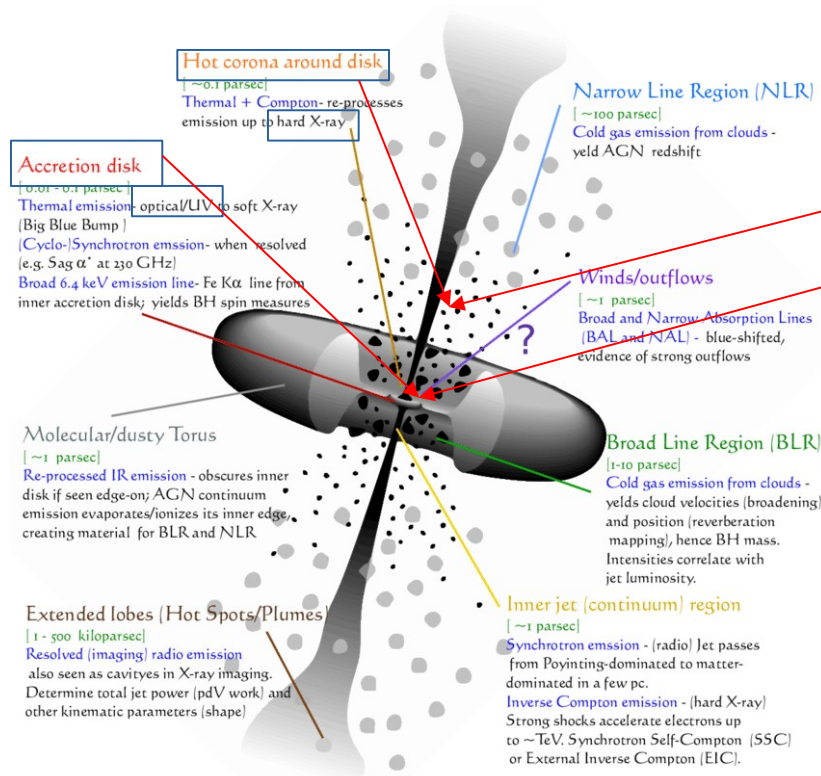
Our results confirm SH0ES local measurements of H_0 results for curvature depend on the approach Λ CDM vs. model-independent reconstructions

to be clarified ...



Hubble diagram at higher redshifts: model independent calibration of quasars

Xiaolei Li,^{1★} Ryan E. Keeley,^{2★} Arman Shafieloo^{ID},^{2,3★} Xiaogang Zheng,⁴ Shuo Cao,⁵ Marek Biesiada^{5,6} and Zong-Hong Zhu⁵

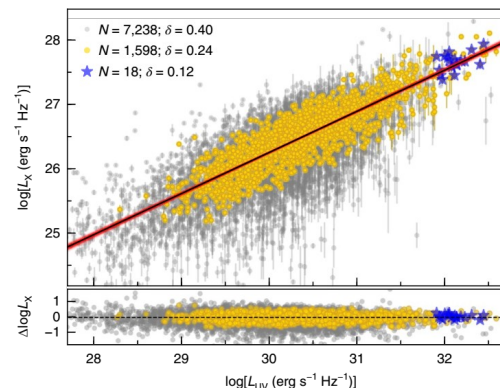


$$\log(L_X) = \gamma \log(L_{UV}) + \beta_1$$

γ from fluxes in redshift bins

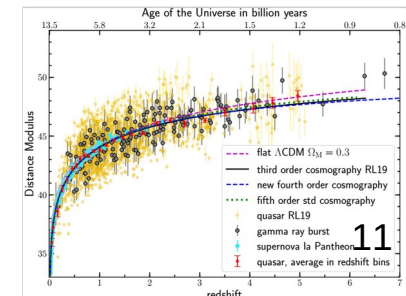
$$\log(F_X) = \gamma \log(F_{UV}) + (2\gamma - 2)\log(D_L) + \beta_2$$

Risaliti & Lusso 2019
Nature Astronomy



$$\beta_2 = \gamma \log(4\pi) - \log(4\pi) + \beta_1.$$

Lusso et al. 2019
A&A Lett. - tension with LCDM



Gaussian Processes reconstruction of cosmic expansion history $H(z)$ from SN Ia Pantheon sample

$$\langle \varphi(s_i) \varphi(s_j) \rangle = \sigma_f^2 \exp\left(-\frac{|s_i - s_j|^2}{2\ell^2}\right)$$

$$\varphi(z) = \ln(H^{\text{mf}}(z)/H(z))$$

$$D_L H_0(z) = (1+z) \int_0^z dz \frac{c}{h(z)}$$

$$\log(F_X)^{\text{SN}} = \gamma \log(F_{\text{UV}}) + (2\gamma - 2)\log(D_L H_0) + \beta,$$

$$\chi^2 = \sum_i \left[\frac{\left(\log(F_X(\gamma, \beta))_i^{\text{SN}} - \log(F_X)_i^{\text{QSO}}\right)^2}{s_i^2} + \ln(s_i^2) \right]$$

$$s_i^2 = \sigma_{\log(F_X)}^2 + \gamma^2 \sigma_{\log(F_{\text{UV}})}^2 + \delta^2$$

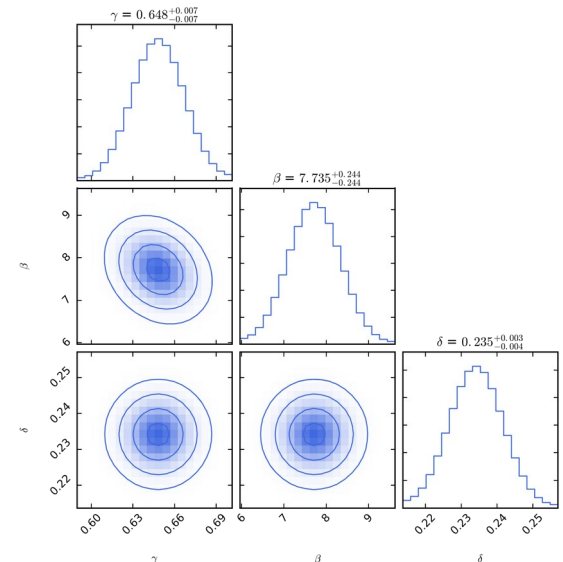
$$\gamma = 0.649 \pm 0.007 \text{ and } \delta = 0.235 \pm 0.04$$

Lusso et al. 2020

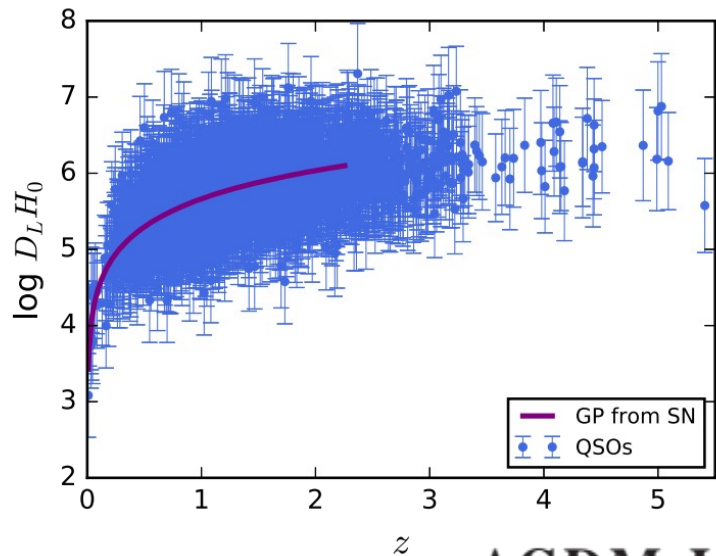
$$\gamma = 0.586 \pm 0.061, \delta = 0.21 \pm 0.06$$

- (i) Draw 1000 unanchored luminosity distances $D_L H_0$ from supernovae data,
- (ii) Calculate the predicted quasar X-ray flux corresponding to these unanchored luminosity distances,
- (iii) Define the likelihood of the quasar parameters,
- (iv) Calculate the posterior distribution of the quasar parameters.

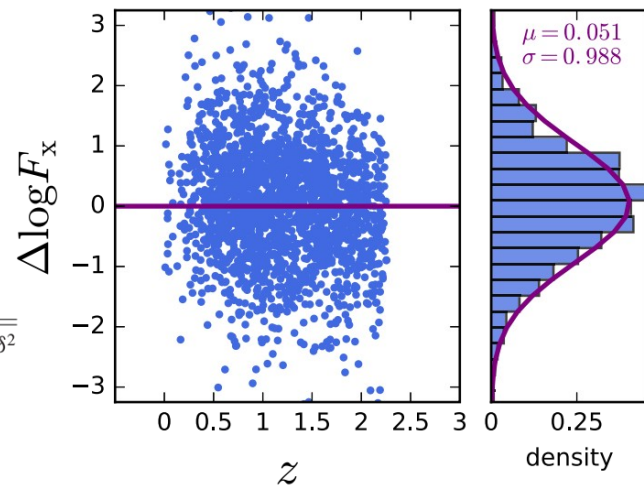
Model independent calibration of quasars



INTERNAL CONSISTENCIES



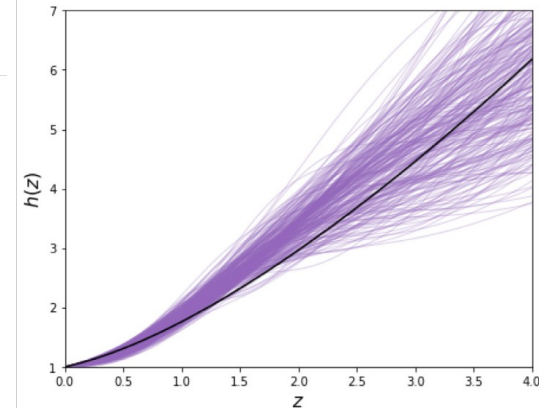
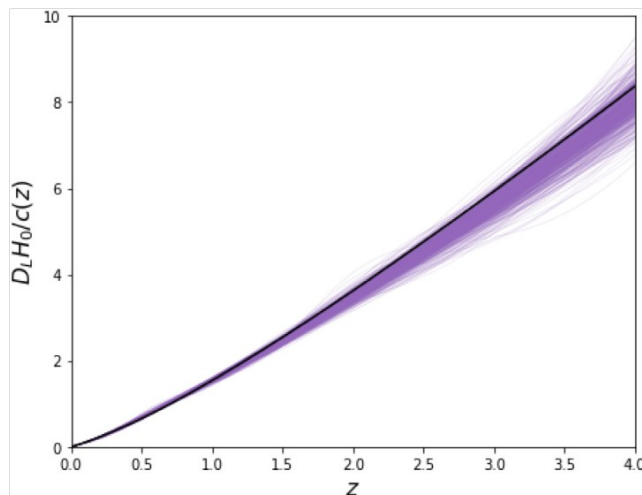
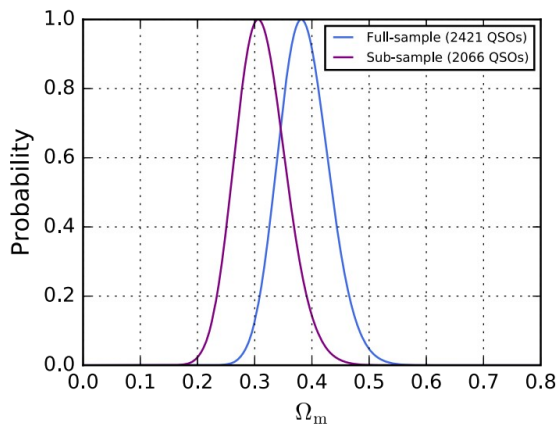
$$\Delta \log(F_X) = \frac{\log(F_X)^{SN} - \log(F_X)^{QSO}}{\sqrt{\sigma_{\log(F_X)}^2 + \gamma^2 \sigma_{\log(F_{UV})}^2 + \delta^2}}$$



ΛCDM INFERENCES

$$\ln \mathcal{L} = -\frac{1}{2} \sum_i \left[\frac{\left(\log(D_L H_0(\Omega_m))_i^{\Lambda\text{CDM}} - \log(D_L H_0)_i^{\text{QSO}} \right)^2}{\sigma_{\log(D_L H_0);i}^2} \right]$$

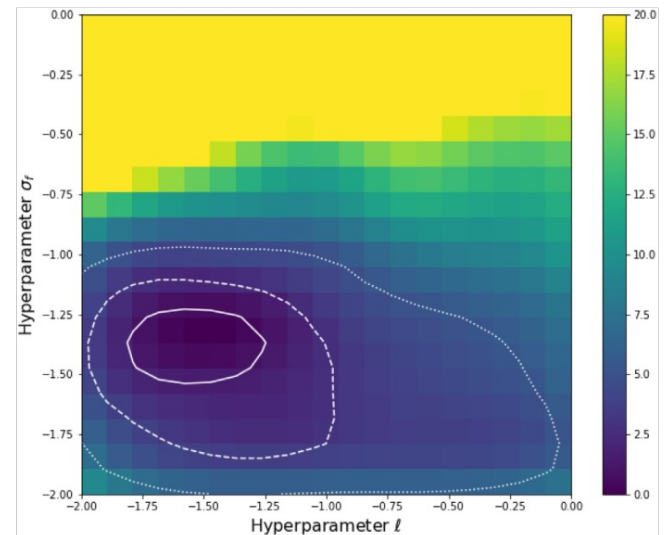
Deviation from Λ CDM seen in Lusso, Risaliti et al. confirmed



Summary:

- * We calibrated QSO UV-X relation with a new model-independent method
- * We confirmed that quasars can be used as new standardizable candles
- * For the full sample we found the deviations from the Λ CDM as in Lusso et al.
- * The 2-3 σ preference of beyond- Λ CDM evolution is supported by posterior distribution of GP hyper-parameters – $\sigma_f > 0$ indicates that data hold more information than can be modeled by input mean function (here assumed Λ CDM)

Further studies are underway



Thank you !